

Calculating pH when given either $[H_3O^+]$ or $[HO^-]$

If hydronium ion concentration is given, simply use calculator and take the negative log of $[H_3O^+]$

$$[H_3O^+] = 3.5 \times 10^{-3} M$$

$$-\log(3.5 \times 10^{-3})$$

$$pH = 2.5$$

If hydroxide ion concentration is given,
First use K_w expression to calculate $[H_3O^+]$
and then take the negative log of $[H_3O^+]$

Given: $[HO^-] = 3.5 \times 10^{-3} M$

First use K_w expression to determine $[H_3O^+]$

$$K_w = [H_3O^+] [HO^-]$$

$$1.0 \times 10^{-14} = [H_3O^+] [HO^-]$$

$$1.0 \times 10^{-14} = [H_3O^+] (3.5 \times 10^{-3})$$

Now rearrange and solve for $[H_3O^+]$

$$\frac{1.0 \times 10^{-14}}{(3.5 \times 10^{-3})} = [H_3O^+] = 2.9 \times 10^{-12}$$

Finally, take $-\log$ of $[H_3O^+]$

$$-\log(2.9 \times 10^{-12})$$

$$pH = 11.5$$

There is a faster method:

Take the $-\log$ of $[HO^-]$, this is called the pOH

Use the K_w expression in log form and rearrange:

$$pOH = -\log(3.5 \times 10^{-3} M) = 2.5$$

$$pOH = 2.5$$

$$K_w = [H_3O^+] [HO^-]$$

$$pK_w = pH + pOH$$

$$14 = pH + 2.5$$

$$pH = 14 - 2.5 = 11.5$$

Calculating pH when strong acid or strong base concentration is given.

Remember, strong electrolytes completely dissociate, thus the concentration of H_3O^+ or OH^- is equal to the starting concentration given in the problem.

Example: 0.15 M HCl gives H_3O^+ concentration of 0.15 M

Take the $-\log$ to get pH: $-\log(0.15) = 0.8$

$$pH = 0.8$$

Example: 0.25 M KOH gives HO^- concentration of 0.25 M

Take the $-\log$ to get pOH: $-\log(0.25) = 0.6$

$$pOH = 0.6$$

$$pH = 14 - pOH$$

$$pH = 13.4$$